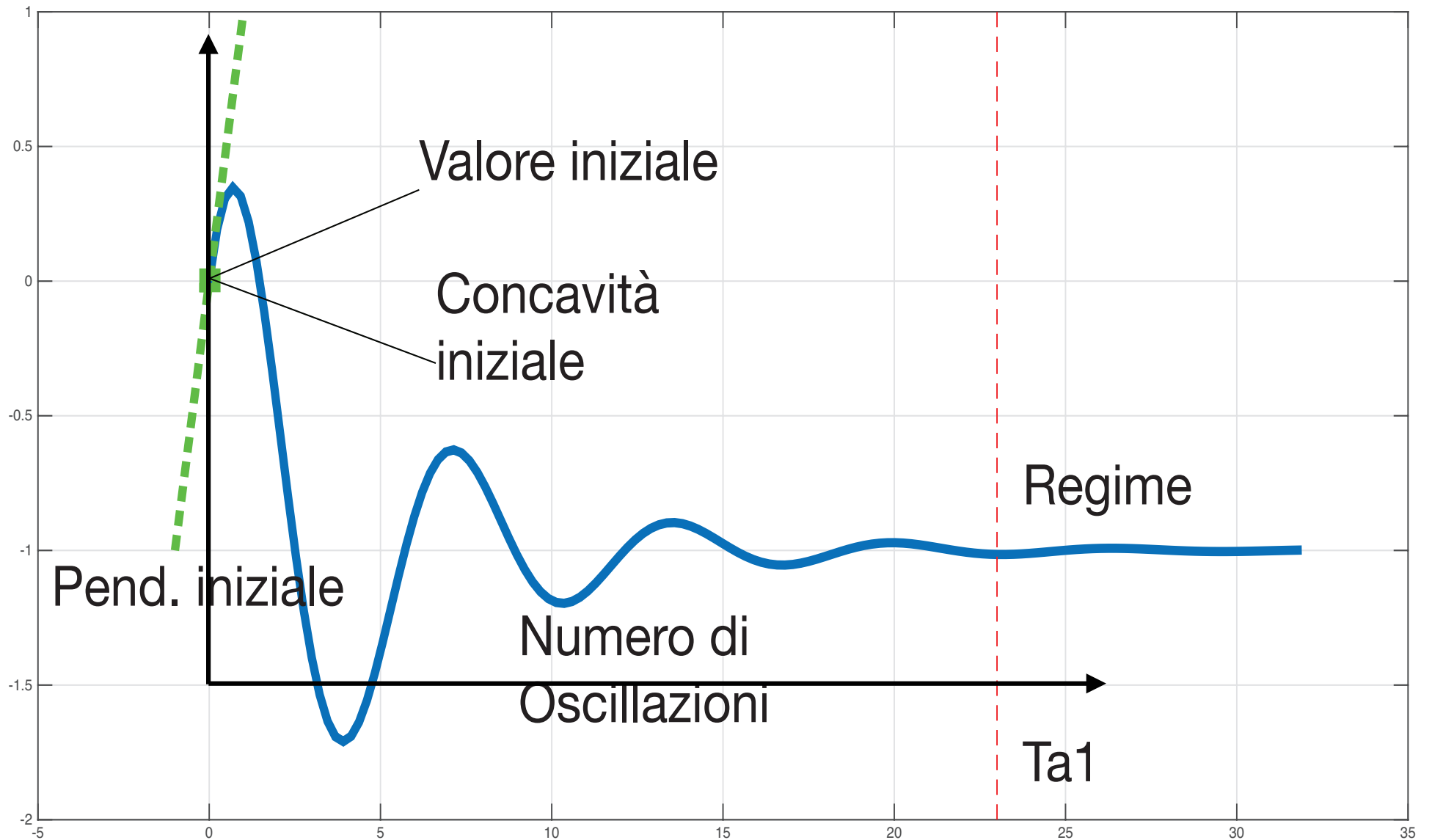


# Automatica

*A.A. 2023/2024*

# **RISPOSTA QUALITATIVA**

# ESEMPIO INTRODUTTIVO



# ESERCIZIO #1

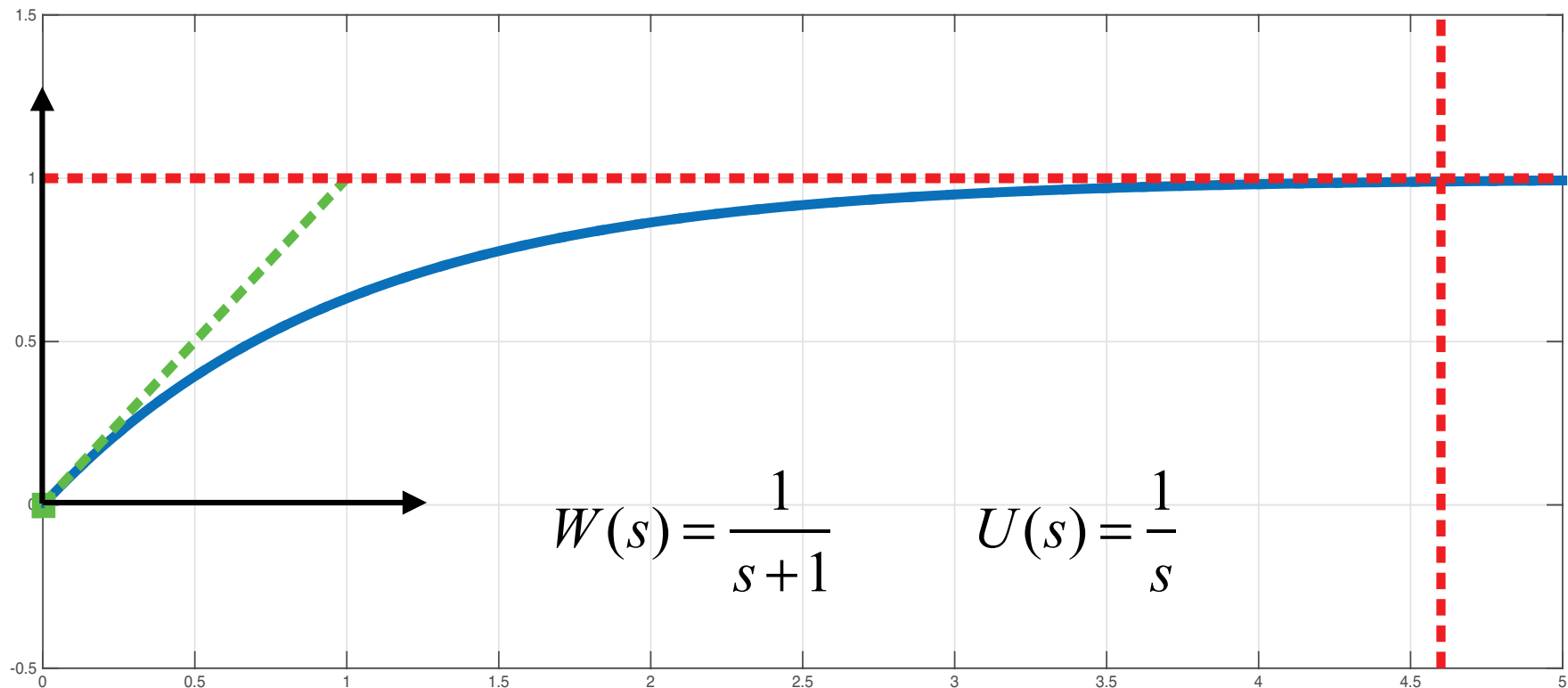
$$y(0) = \lim_{s \rightarrow \infty} sY(s) = 0$$

$$\dot{y}(0) = \lim_{s \rightarrow \infty} s \left[ sY(s) - y(0) \right] = 1$$

$$\ddot{y}(0) = \lim_{s \rightarrow \infty} s \left[ s \left( sY(s) - y(0) \right) - \dot{y}(0) \right] < 0$$

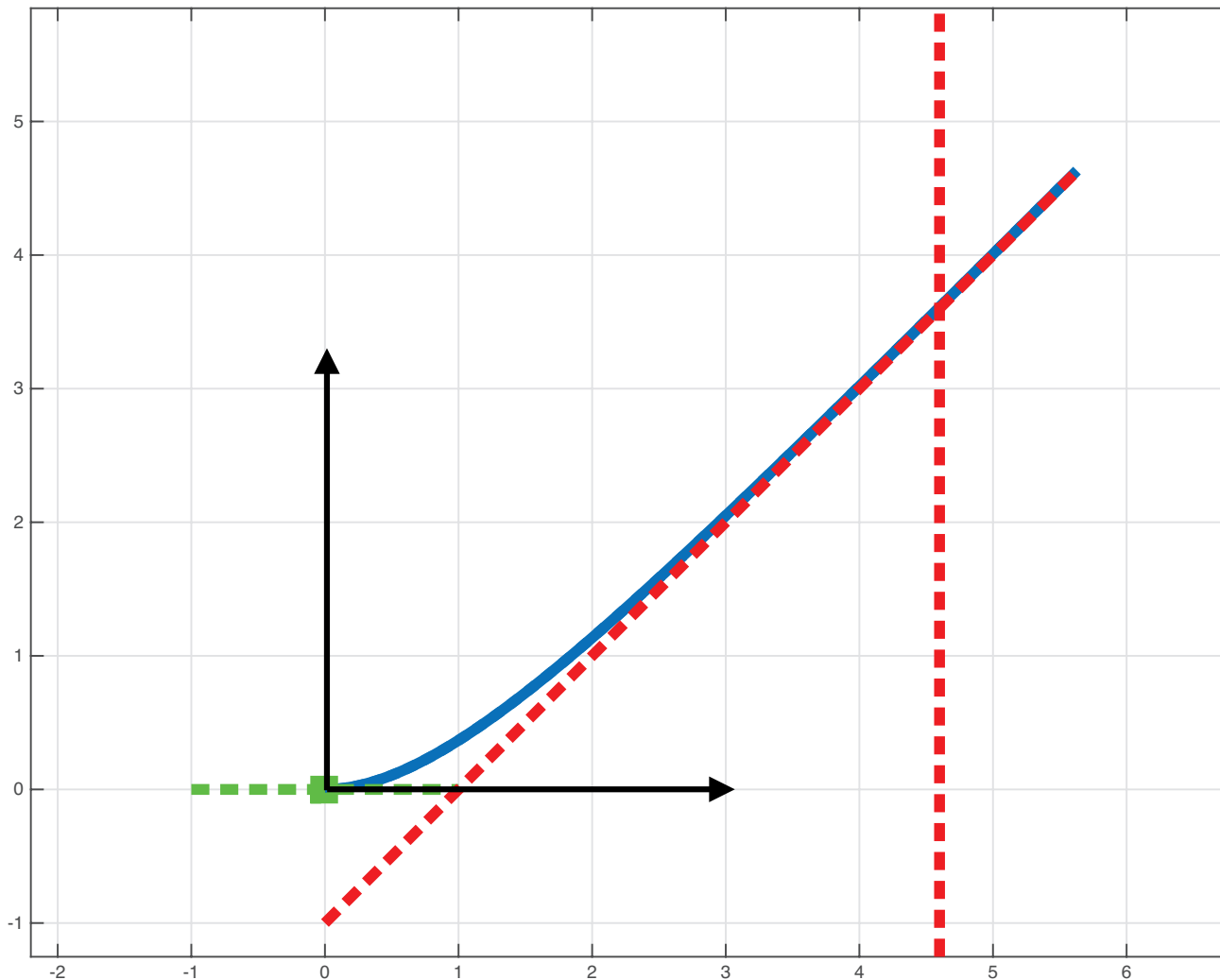
$$y_{\infty}(t) = 1$$

$$T_{a1} = 4.6$$



# ESERCIZIO #2

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$$W(s) = \frac{1}{s+1}$$

$$U(s) = \frac{1}{s^2}$$

$$y(0) = 0$$

$$\dot{y}(0) = 0$$

$$\ddot{y}(0) > 0$$

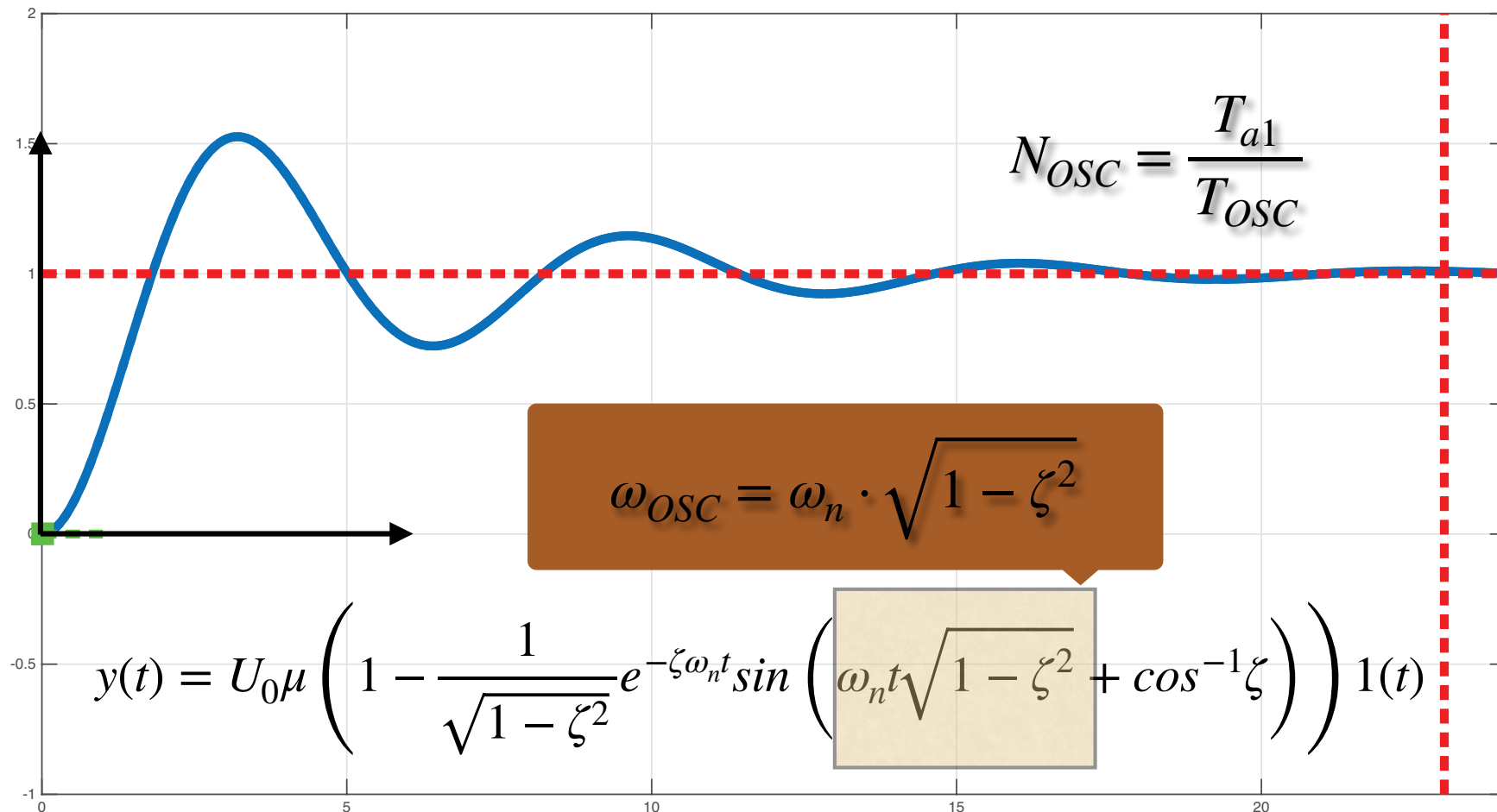
$$y_{\infty}(t) = t - 1$$

$$T_{a1} = 4.6$$

# ESERCIZIO #3

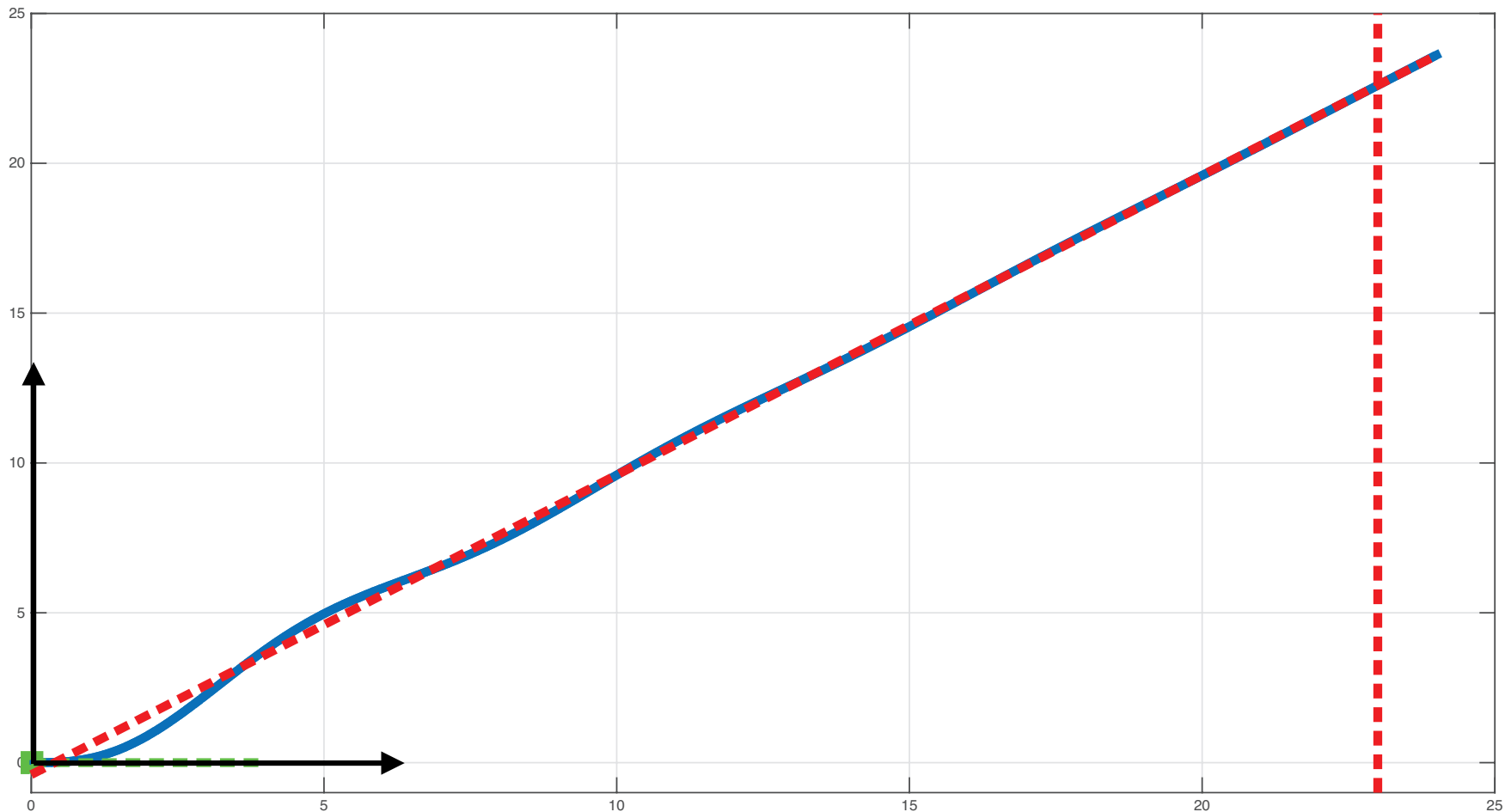
$$W(s) = \frac{1}{s^2 + .4s + 1} \quad U(s) = \frac{1}{s} \quad y(0) = 0 \quad \dot{y}(0) > 1 \quad T_{a1} = 23$$

$$\dot{y}(0) = 0 \quad y_{\infty}(t) = 1 \quad N_{osc} = 3.58$$



# ESERCIZIO #4

$$W(s) = \frac{1}{s^2 + .4s + 1}, U(s) = \frac{1}{s^2} \quad \begin{array}{l} y(0) = 0 \\ \dot{y}(0) = 0 \end{array} \quad \begin{array}{l} \dot{y}(0) = 0 \\ y_{\infty}(t) = t - 0.4 \end{array} \quad \begin{array}{l} T_{a1} = 23 \\ N_{osc} = 3.58 \end{array}$$



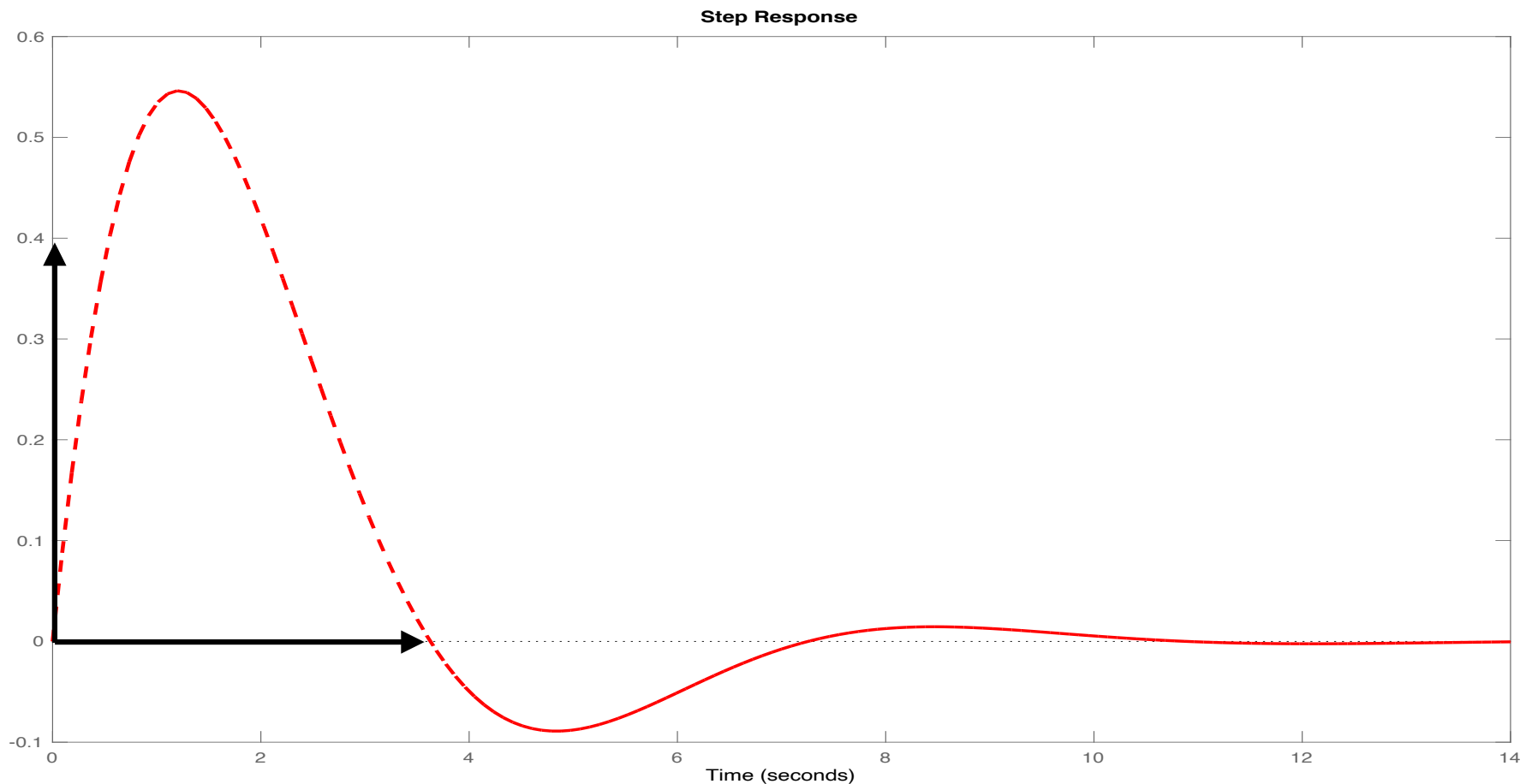
# ESERCIZIO #5

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$$W(s) = \frac{s}{s^2 + s + 1}, U(s) = \frac{1}{s}$$

$$y(0) = 0 \quad \ddot{y}(0) < 0 \quad T_{a1} = 9.2$$

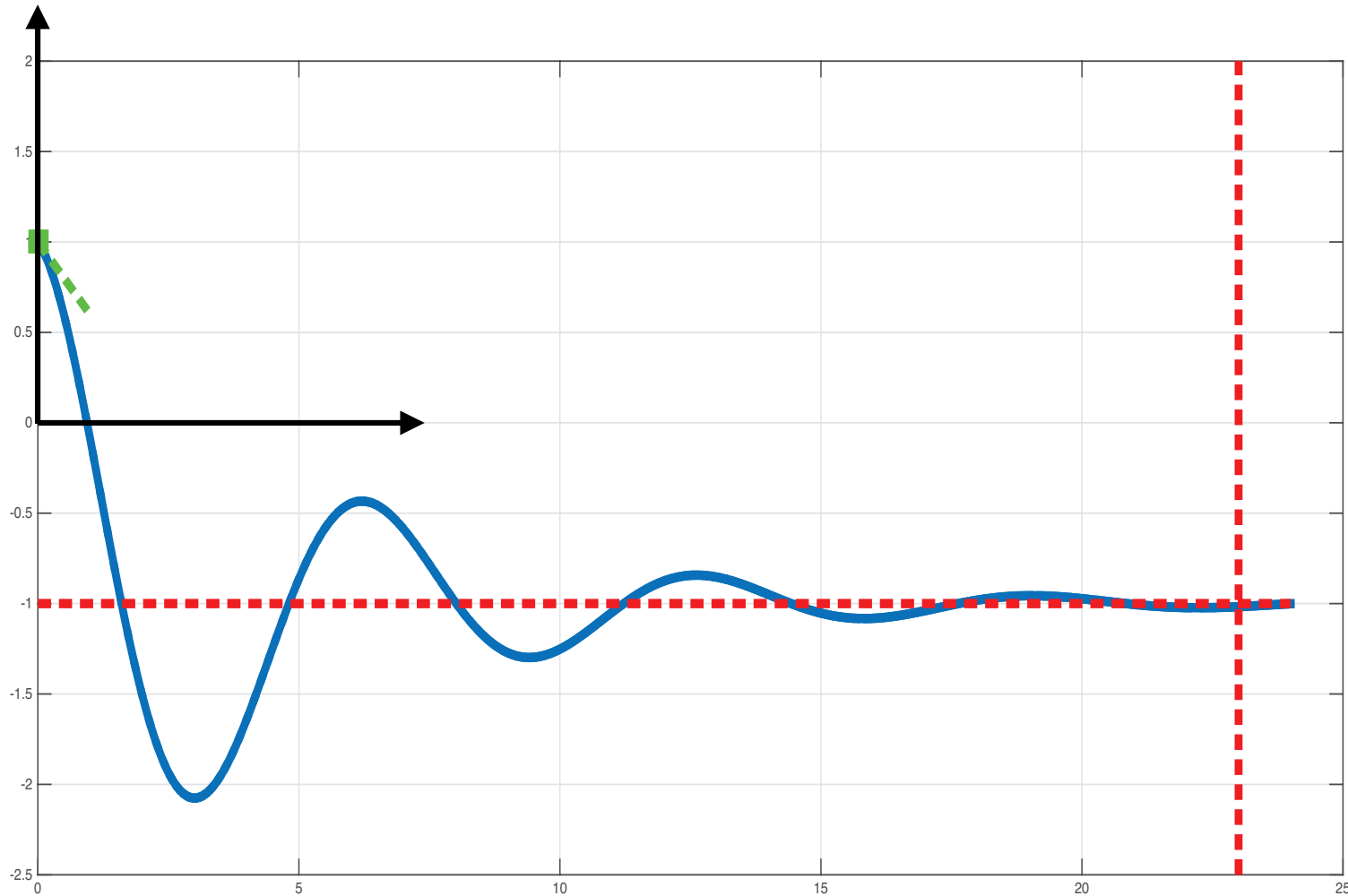
$$\dot{y}(0) = 1 \quad y_{\infty}(t) = 0 \quad N_{osc} = 1.26$$





# ESEMPIO #6

$$W(s) = \frac{(s+1)(s-1)}{s^2 + .4s + 1} \quad U(s) = \frac{1}{s}$$



$$y(0) = 1$$

$$\dot{y}(0) = -0.4$$

$$\ddot{y}(0) < 0$$

$$y_{\infty}(t) = -1$$

$$T_{a1} = 23$$

$$N_{osc} = 3.58$$